Yield Modes in a Coated Sphere Compressed by a Rigid Flat

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Motivation

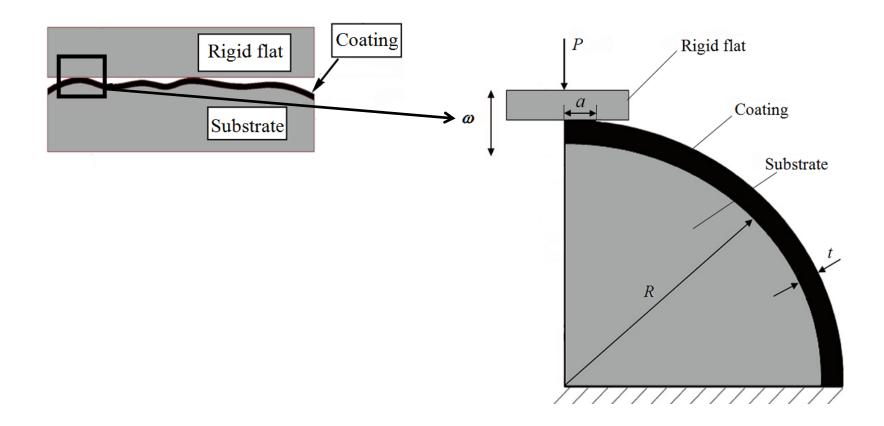






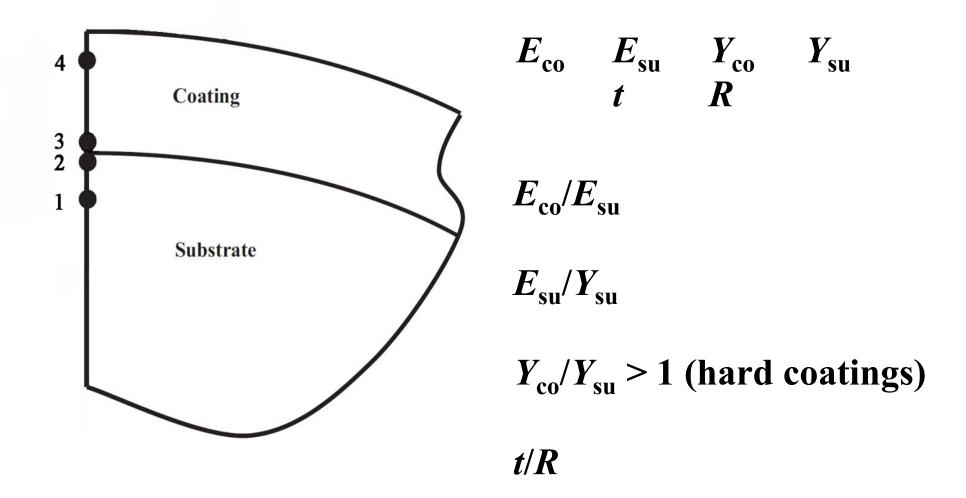


Single asperity of contacting coated rough surfaces

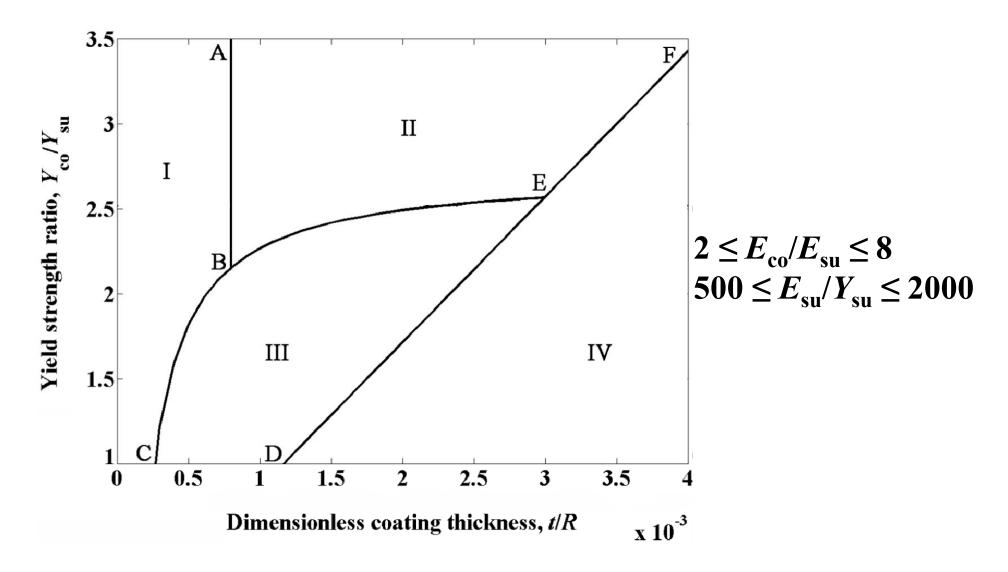


[1] J. Greenwood, J. Williamson, Contact of nominally flat surfaces, The Royal Society (London) 295 (1966), 300-319.

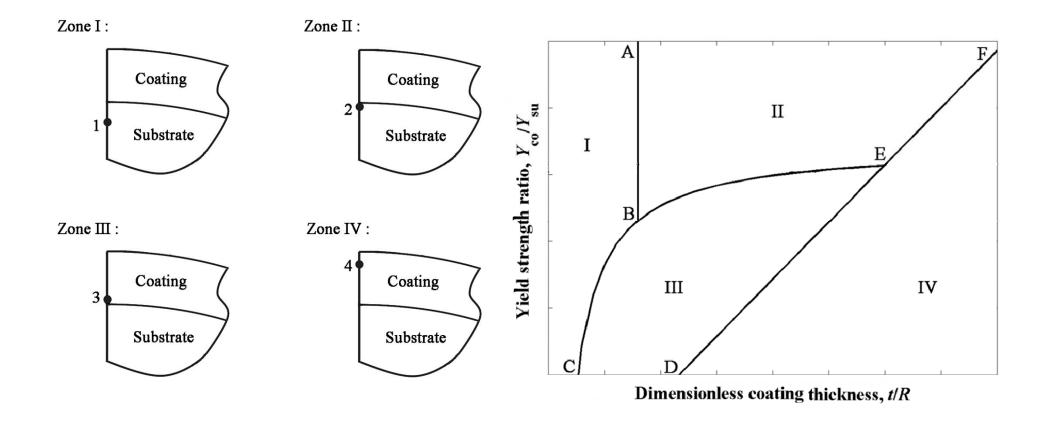
Yield inception locations



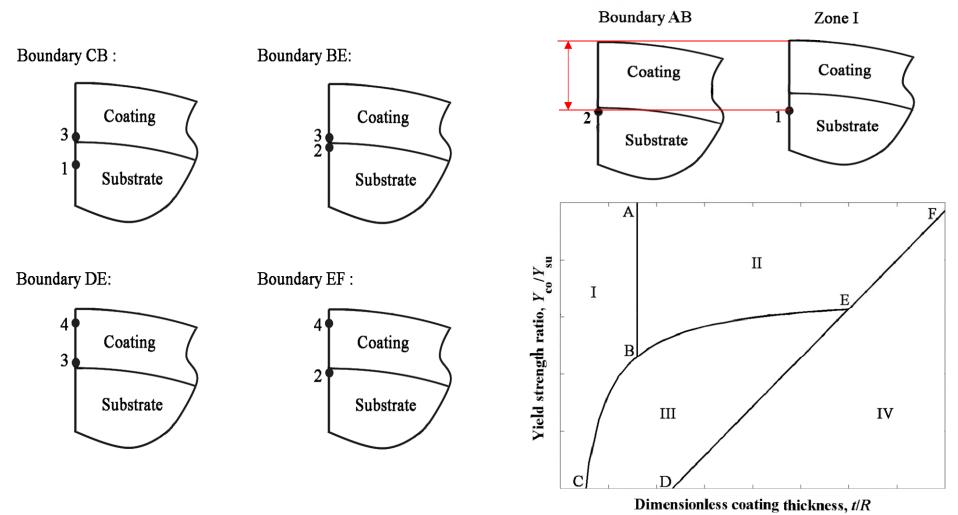
The yield map for $E_{co}/E_{su} = 4$ and $E_{su}/Y_{su} = 1000$



The yield mode in each zone

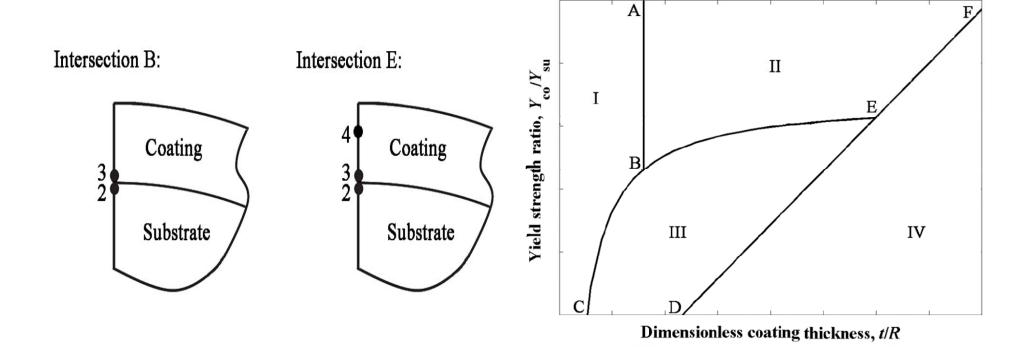


The yield mode on each zone boundary



[2] R. Goltsberg and I. Etsion, A model for the weakening effect of very thin hard coatings, Wear 308 (2013) 10-16.

The yield mode at intersection points



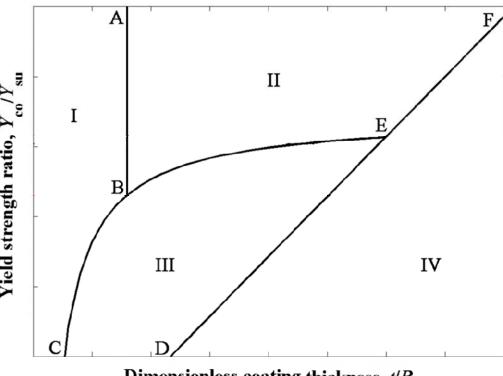
Determination of a yield map

$$\left(\frac{t}{R}\right)_{CBE} = \frac{0.15}{\left[0.912 - \left(\frac{Y_{co}}{Y_{su}}\right)\left(\frac{E_{co}}{E_{su}}\right)^{-0.787}\right]\left(\frac{E_{su}}{Y_{su}}\right)}$$

$$\left(\frac{t}{R}\right)_{DEF} = 1.35 \left(\frac{Y_{co}}{Y_{su}}\right) \left(\frac{E_{co}}{E_{su}}\right)^{-0.6} \left(\frac{E_{su}}{Y_{su}}\right)^{-0.9}$$

$$\left(\frac{t}{R}\right)_{AB} = \frac{1.066}{\left(E_{co}/E_{co}/E_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_{co}/Y_$$

$$\left(\frac{t}{R}\right)_{AB} = \frac{1.066}{\left(E_{co} / E_{su}\right)^{0.225} \left(E_{su} / Y_{su}\right)}$$



Determination of the yield mode in a coated system

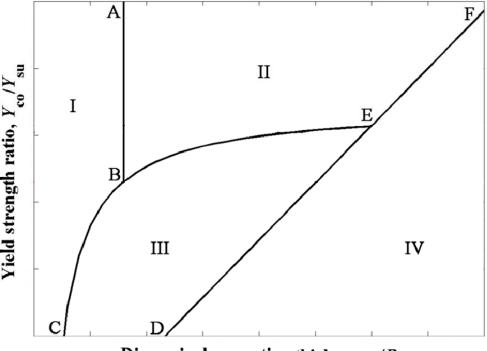
$$\left(\frac{Y_{co}}{Y_{su}}\right)_{E} = \left[0.456 + \sqrt{0.208 - \frac{1}{9} \left(\frac{E_{co}}{E_{su}}\right)^{-0.187} \left(\frac{E_{su}}{Y_{su}}\right)^{-0.1}}\right] \left(\frac{E_{co}}{E_{su}}\right)^{0.787}$$

$$\left(\frac{Y_{co}}{Y_{su}}\right)_{B} = 0.912 \left(\frac{E_{co}}{E_{su}}\right)^{0.787} - 0.141 \left(\frac{E_{co}}{E_{su}}\right)^{1.012}$$

$$\frac{X_{co}}{E_{su}}$$

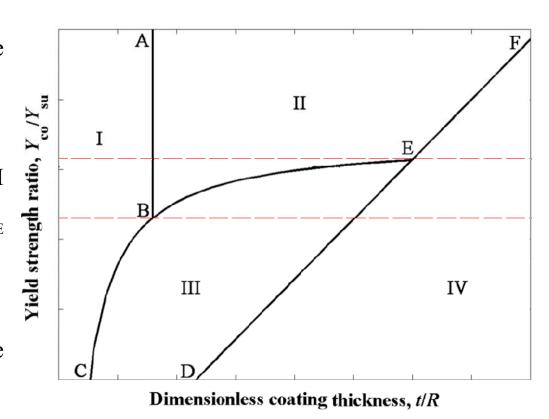
$$\frac{X_{co}}{E_{su}}$$

$$\frac{X_{co}}{E_{su}}$$

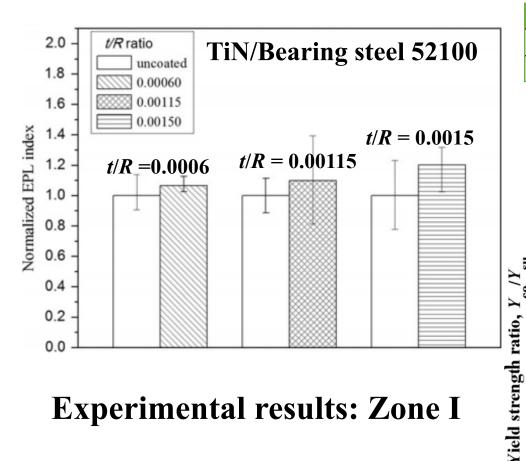


Determination of the yield mode in a coated system

- 1) $Y_{co}/Y_{su} > (Y_{co}/Y_{su})_E$ I, II or IV Compare t/R with $(t/R)_{AB}$ and $(t/R)_{DEF}$
- 2) $(Y_{co}/Y_{su})_{B} < Y_{co}/Y_{su} < (Y_{co}/Y_{su})_{E} I$, II, III or IV. Compare t/R with $(t/R)_{AB}$, $(t/R)_{CBE}$ and $(t/R)_{DEF}$
- 3) $Y_{co}/Y_{su} < (Y_{co}/Y_{su})_B$ I, III or IV Compare t/R with $(t/R)_{CBE}$ and $(t/R)_{DEF}$

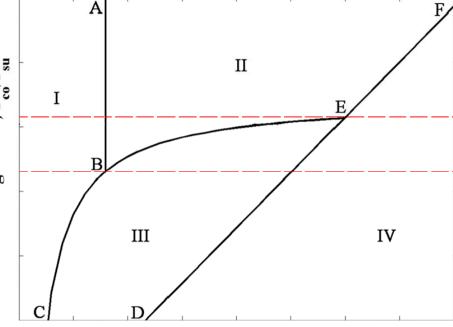


Comparison with experimental results



Actual parameters			Calculated parameters	
$E_{\rm co}/E_{\rm su}$	$E_{\rm su}/Y_{\rm su}$	$Y_{\rm co}/Y_{\rm su}$	$(Y_{\rm co}/Y_{\rm su})_{\rm E}$	$(t/R)_{AB}$
1.65	140	5.24	1.24	0.0068

Theoretical results: Zone I



Experimental results: Zone I

[2] R. Goltsberg and I. Etsion, A model for the weakening effect of very thin hard coatings, Wear 308 (2013) 10-16.

Dimensionless coating thickness, t/R

[3] X. Huang et al., Experimental study of a potential weakening effect in spheres with thin hard coatings, Wear 296 (2012) 590-597.

Conclusion

- Four typical locations of yield inception on the axis of symmetry were found.
- Different yield modes, characterized by the yield inception locations, were found and can be presented in a yield map as a function of $Y_{\rm co}/Y_{\rm su}$ and t/R for given $E_{\rm co}/E_{\rm su}$ and $E_{\rm su}/Y_{\rm su}$.
- Each of the zones corresponds to a yield mode with a single yield inception location. Four of the zone boundaries correspond to yield modes with double simultaneous yield inception locations and one of the intersection points has a yield mode with triple simultaneous yield inception locations.
- Universal dimensionless expressions for the zone boundaries were derived that enable to determine the yield mode of any coated system based on the material properties and dimensionless coating thickness. The validity of the determination was verified by a comparison with an experimental study.

Thank you for your attention!